

**MAE 119 WINTER 2015 PROFESSOR G.R. TYNAN  
QUIZ 5: SOLAR THERMAL POWER TECHNOLOGY**

**CLOSED BOOK CLOSED NOTES.**

One significant figure will suffice for your answers.

A solar thermal power plant is to be built in a region that has on average a Direct Normal Incidence (DNI) of  $500 \text{ W/m}^2$  and a Diffuse Horizontal Irradiance (DHI) of  $500 \text{ W/m}^2$  for 10 hours per day. These values then go to zero for the other 14 hours per day. The plant will use a heat engine that has a conversion efficiency of 40%. It is desired that the plant produce 100 MW of electricity continuously.

- (a) What is the minimum light collecting area required for these specifications?  
10 points.
- (b) How much energy needs to be stored for subsequent use in producing electricity at night? 10 points.
- (c) Assuming that a thermal energy storage system is used with a thermal storage medium having a specific heat  $C_p = 1 \text{ kJ/kG-deg K}$  and a density  $\rho = 3000 \text{ kG/m}^3$  estimate the volume of the thermal storage system so that the characteristic stored energy decay time exceeding 24 hours? 10 points.

*Hint:* Recall that the power balance for the thermal storage system is given

$$\text{as } \rho C_p V \frac{\partial T}{\partial t} = P_{in} - \frac{1}{\eta_{th}} P_{out}$$

- (d) Explain in words why it would be useful to have such a long thermal energy decay time.

## Quiz 5 Solution

a) Need 100 MW

In steady state :  $P_{in} = \frac{P_{out}}{\eta}$

$$P_{in} = I_{DN I} A$$

$$\therefore A = \frac{P_{out}}{\eta I} = \frac{100 \times 10^6 \text{ W}}{500 \text{ W} (0.4) \text{ m}^2}$$

$$= 0.5 \times 10^6 \text{ m}^2 = 0.5 \text{ km}^2$$

b) to get 100 MW at  $\eta = 40\%$ .

$$\text{we need } \frac{100 \times 10^6 \text{ W}}{0.4} = \frac{100 \times 10^6 \text{ W}}{40 \times 10^{-2}} = 2.5 \times 10^8 \text{ W}$$

which, sustained for the entire night is

$$(14 \text{ hrs} \cdot 2.5 \times 10^8 \text{ W}) = 35 \times 10^8 \text{ Whr} = \boxed{3.5 \text{ GWhr}}$$

$$\approx \boxed{4 \text{ GWhr}}$$

↑ okay

$$c) \rho C_p V \frac{dT}{dt} = P_{in} - \frac{1}{\eta} P_{out}$$



$$\rho C_p V dT = - \frac{P_{out}}{\eta} dt$$

$$\int_{T(t=0)}^{T(t)} dT = \frac{-P_{out}}{\eta \rho C_p V} \int_{t=0}^t dt$$

$$\Delta T = \frac{-P_{out}}{\eta \rho C_p V} \Delta t$$

$P_{in}$  can be assumed zero at night with no mention of another generator.

$P_{out}$  is a constant 100 MW.

c) cont. ...

$$\Delta t = \underbrace{-\eta \frac{C_p \rho V \Delta T}{P_{out}}}_{\tau}$$

$\tau$  characteristic time

$$\tau = 24 \text{ h} \cdot \frac{3600 \text{ s}}{\text{h}} = 8 \times 10^4 \text{ s}$$

$$* V = \frac{P_{out} \tau}{\eta C_p \rho V \Delta T}$$

\* Either solve for  $V$  in terms of  $^{\circ}\text{K}$  (i.e. for  $1^{\circ}\text{K}$  of temperature difference) or assume  $\Delta T \approx 100 - 300^{\circ}\text{K}$ .

$$V = \frac{(100 \times 10^6 \text{ W})(8 \times 10^4 \text{ s})}{(0.4)(1000 \frac{\text{J}}{\text{kgK}})(3000 \text{ kg/m}^3)(\Delta T \text{ K})}$$
$$= \frac{800 \times 10^{10}}{12 \times 10^5 (\Delta T)} \approx \boxed{8 \times 10^6 \text{ m}^3 \cdot ^{\circ}\text{K} \Delta T}$$
$$\boxed{V = 3 \times 10^4 - 8 \times 10^4 \text{ m}^3}$$

D) The long decay time is useful for providing power at night (14 hrs), <sup>during</sup> intermittent days with low DNI, and in case of unforeseen contrails or clouds. This added storage effectively boosts the capacity factor of the system and provides flexibility with added dispatchability.